

**True/False** - No explanation needed. (2pts)

1. For any events  $A, B \subseteq \Omega$ , we have  $P(A \cup B) + P(A \cap B) = P(A) + P(B)$ . True/False
2. Sending off newly-married couples to honeymoons on different planets around the universe will provide a counterexample for the even version of the “Odd-pie fight” problem. True/False

**Problems** - Need justification. No justification means **zero!**

1. What is the probability that a 5-card poker hand contains no aces? (A 5-card poker hand consists of 5 cards from a 52 card standard deck.) (5pts)

2. Prove that

$$1 \cdot 2 + 2 \cdot 3 + \cdots + n \cdot (n + 1) = \frac{n(n + 1)(n + 2)}{3}$$

for all  $n \geq 1$ , by using mathematical induction. (5pts)