1   Z-Test

1. When Thanos snapped his fingers, everyone had a $p = 0.5$ chance of disintegrating. I think that this probability was much lower for the original Avengers. Out of the 6 of them, no one got disintegrated. Can you reject the null hypothesis that there was a $p = 0.5$ chance of each of them disintegrating with an $\alpha = 0.05$?

2. An infomercial claims that a miracle drug will cause you to grow all your hair back. There are 25 brave participants and surprisingly 7 people regrew their hair. If normally 10% of people regrow their hair, can you say that this drug worked?

3. You flip a coin 100 times and get 55 heads. Can you say that it is biased towards heads? (use $\alpha = 0.05$)

4. An infomercial claims that a miracle drug will cause you to grow all your hair back. There are 100 brave participants and this time 20 people regrew their hair. If normally 10% of people regrow their hair, can you say that this drug worked?

2   T-Test

Concept:What is the t-statistic, and what is it used for?

For a sample of size n, the t-statistic is a measure of how far the sample mean Y_n lies from the hypothesized population mean μ_0, measured in units of the standard error in the mean $s/\sqrt{n}$. The t-statistic is given by

$$T_{n-1} = \frac{Y_n - \mu_0}{s/\sqrt{n}}$$

It is used during hypothesis testing to determine whether the sample data are compatible with the null hypothesis. It usually deal with the case that has small sample size.

1. The heart rates of 40 patients in an ICU have mean 95.3beats/min and standard deviation 16.9 beats/min. Are heart rates from ICU patients unusual given normal heart rate has mean of 72 beats/min?

   (a) What is the degree of freedom?
   (b) What is the t-statistics?